

MAT2440, Quiz2, Spring2025

ID: _____ Name: _____

1. Translate the given statement into propositional logic using the propositions provided:

‘You can see the movie **only if** you are over 18 years old or you have the permission of a parent.’ Express your answer in terms of **m**: ‘You can see the movie,’ **e**: ‘You are over 18 years old,’ and **p**: ‘You have the permission of a parent.’

Sol: since a only if b is $a \rightarrow b$, then we have

$$m \rightarrow (e \vee p)$$

2. Use identities to prove De Morgan’s law for 3 propositions:

$$\neg(p \wedge q \wedge r) = (\neg p) \vee (\neg q) \vee (\neg r).$$

Sol: $\neg(p \wedge q \wedge r) \equiv \neg(p \wedge q \wedge r)$
 $\equiv \neg(p \wedge q) \vee \neg r$ by De Morgan's law
 $\equiv \neg p \vee \neg q \vee \neg r$ by De Morgan's law.

3. Show that $(p \rightarrow r) \vee (q \rightarrow r)$ and $(p \wedge q) \rightarrow r$ are logically equivalent.

p	q	r	$p \rightarrow r$	$q \rightarrow r$	$(p \rightarrow r) \vee (q \rightarrow r)$	$(p \wedge q)$	$(p \wedge q) \rightarrow r$
T	T	T	T	T	T	T	T
T	T	F	F	F	F	T	F
T	F	T	T	T	T	F	T
T	F	F	F	T	T	F	T
F	T	T	T	T	T	F	T
F	T	F	T	F	T	F	T
F	F	T	T	T	T	F	T
F	F	F	T	T	T	F	T

Since $(p \rightarrow r) \vee (q \rightarrow r)$ has the same truth values of $(p \wedge q) \rightarrow r$, they are equivalent.