

Quiz6, MAT 1375 Professor Chiu

ID: _____

Name: Sol

- This quiz consists of 2 sets of questions, each worth 5 points, for a total of 10 points.
- You have 10 minutes to complete the quiz.
- Scientific calculators are allowed.
- Wishing you success.

True or False questions:

1. T Given a function $f(x)$. If $f(-x) = f(x)$, then $f(x)$ is an even function.
2. F Given a function $f(x)$. If $f(-x) = -f(x)$, then $f(x)$ is an ~~even~~ odd function.
3. T The function $f(x) = x^3$ is an odd function.
4. T The parabola $y = -(x + 2)^2$ is the reflection of $y = (x + 2)^2$ about the x -axis.
5. T The parabola $y = x^2$ is the reflection of $y = x^2$ about the y -axis.

Show all your work and justify your answer:

6. Given a function $f(x) = 3x^4 - 4x^2 + 5$. Determine if the function f is even, odd, or neither.

To check if $f(x)$ is even, odd, or neither,

We first replace x by " $-x$ " and get

$$\begin{aligned} f(-x) &= 3 \cdot (-x)^4 - 4(-x)^2 + 5 \\ &= 3x^4 - 4x^2 + 5. \end{aligned}$$

Since $f(-x) = 3x^4 - 4x^2 + 5 = f(x)$, then $f(x)$ is even.