

# Quiz10, MAT 1375 Professor Chiu

ID: \_\_\_\_\_

Name: \_\_\_\_\_

- This quiz consists of 2 sets of questions for a total of 10 points.
- You have 15 minutes to complete the quiz.
- Scientific calculators are allowed.
- Wishing you success.

True or False questions:

1. F  $f(x) = 2x^2 + x^5$  is a polynomial with degree 2.   
*Handwritten notes: leading term  $x^5$ , leading coefficient = 1, degree = 5*
2. T Odd-degree polynomial functions have graphs with opposite behavior at each end.
3. T Even-degree polynomial functions have graphs with the same behavior at each end.
4. F A root of a polynomial  $f(x)$  appears as the  $x$ -intercept of the graph of  $f(x)$ .   
*Handwritten note: x-intercept*

Show all your work and justify your answer:

5. Work out the following problems about the polynomial function  $f(x) = -3(x-1)^3(2x+4)^2$ .

(1.) (2pt) Find the leading term of  $f(x)$ . Using **the leading coefficient test** to determine the **end behavior** of  $f(x)$

$f(x) = -3(x-1)(x-1)(x-1)(2x+4)(2x+4)$

leading term:  $(-3) \cdot x \cdot x \cdot x \cdot 2x \cdot 2x = -12x^5$

leading coefficient:  $-12 \Rightarrow -12$  is negative

degree:  $5 \Rightarrow 5$  is an odd number

End behavior:  $(\uparrow, \downarrow)$

$x \rightarrow -\infty, f \rightarrow \infty$

$x \rightarrow \infty, f \rightarrow -\infty$

(2.) (2pt) Find the **zeros** of  $f(x)$  and their **multiplicities**.

zeros of  $f(x) \Rightarrow x$  makes  $f(x) = 0 \Rightarrow f(x) = -3(x-1)^3(2x+4)^2 = 0$

zero  $x = 1$  ( $(x-1)=0 \Rightarrow x=1$ ),  $x = -2$  ( $2x+4=0 \Rightarrow x=-2$ )

multiplicity  $3$  (times),  $2$  (times)

(How many times the zero repeat)

(3.) (2pt) Find the **y-intercept** of  $f(x)$ .

y-intercept of  $f(x) \Rightarrow$  the value of  $f(x)$  when  $x=0$

$f(0) = -3(0-1)^3(2 \cdot 0 + 4)^2 = -3 \cdot (-1)^3 \cdot (4)^2 = 48$