

9 Quiz 9 MAT 1275 Professor Chiu

Name: _____

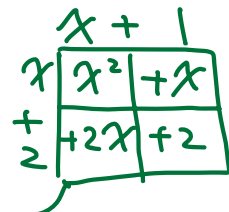
- This quiz consists of **2** questions, each worth 5 points for a total of **10** points.
- You have **15** minutes to complete the quiz.
- Show all work and justify your answers.
- Scientific calculators are allowed.
- Wishing you success.

1. Subtract and simplify:

$$\frac{x-7}{(x+2)(x-1)} - \frac{x+1}{(x-1)(x)}$$

① Copy the part it does NOT have to get the common denominator

$$\frac{(x-7)x}{(x+2)(x-1)x} - \frac{(x+1)(x+2)}{(x-1)(x)(x+2)}$$



$$= \frac{x^2 - 7x - (x^2 + 3x + 2)}{(x+2)(x-1)x}$$

② Combine two fractions

$$= \frac{x-7}{x} \begin{array}{|c|} \hline x^2 \\ \hline -7x \\ \hline \end{array}$$

$$= \frac{x^2 - 7x - x^2 - 3x - 2}{(x+2)(x-1)x} = \frac{-10x - 2}{(x+2)(x-1)x}$$

PLEASE TURN OVER FOR THE NEXT QUESTION.

2. Simplify:

① Numerator: $\frac{2}{x-2} + \frac{1}{x+2}$

$$= \frac{2(x+2)}{(x-2)(x+2)} + \frac{1(x-2)}{(x+2)(x-2)}$$

$$= \frac{2x+4}{(x-2)(x+2)} + \frac{x-2}{(x+2)(x-2)}$$

$$= \frac{2x+4+(x-2)}{(x-2)(x+2)}$$

$$= \frac{3x+2}{(x-2)(x+2)}$$

② Denominator: $1 - \frac{x}{2-x}$

$$= \frac{1}{1} - \frac{x}{2-x}$$

$$= \frac{1 \cdot (2-x)}{1 \cdot (2-x)} - \frac{x}{2-x}$$

$$= \frac{2-x-x}{2-x}$$

$$= \frac{2-2x}{2-x}$$

$$\frac{\frac{2}{x-2} + \frac{1}{x+2}}{1 - \frac{x}{2-x}}$$

③ $\frac{\frac{2}{x-2} + \frac{1}{x+2}}{1 - \frac{x}{2-x}}$

$$= \left(\frac{2}{x-2} + \frac{1}{x+2} \right) \div \left(1 - \frac{x}{2-x} \right)$$

by ① $\left(\frac{3x+2}{(x-2)(x+2)} \right) \div \left(\frac{2-2x}{2-x} \right)$ by ②

$$= \frac{(3x+2)}{(x-2)(x+2)} \cdot \frac{(2-x)}{(2-2x)}$$

↓ "flip"

$$= \frac{(3x+2)}{(x-2)(x+2)} \cdot \frac{-(x-2)}{(2-2x)}$$

$$= \frac{-\cancel{(3x+2)} \cdot \cancel{(x-2)}}{\cancel{(x-2)}(x+2)(2-2x)}$$

$$= \frac{- (3x+2)}{(x+2)(2-2x)}$$

$$\begin{aligned} 2-x &= -1 \cdot (-2+x) \\ &= -1 \cdot (x-2) \\ &= -(x-2) \end{aligned}$$