

Indeterminate form:

$$\underbrace{\frac{0}{0}, \frac{\infty}{\infty}}_{\text{Math 1450, Honor Calculus Practice 6, Fall 2016.}}, \underbrace{0 \cdot \infty, \infty - \infty}, \underbrace{0^0, 1^\infty, \infty^0}$$

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($\frac{0}{0}$) 1. Calculate the limit $\lim_{x \rightarrow 0} \frac{e^x - 1}{10 \ln(1+x)}$. $\stackrel{(\frac{0}{0})}{\downarrow} \lim_{x \rightarrow 0} \frac{e^x}{\frac{10}{1+x}} = \frac{1}{10}$

(X) 2. Calculate the limit $\lim_{x \rightarrow 0} \frac{4x - \sin(\pi x)}{2x^2 - 1} = \frac{0}{-1} = 0$

$\frac{4x - \sin(\pi x)}{2x^2 - 1}$ is NOT one of the indeterminate form.

($\frac{\infty}{\infty}$) 3. Calculate the limit $\lim_{x \rightarrow \infty} \frac{\ln(x^7)}{x}$. $\stackrel{(\frac{\infty}{\infty})}{\downarrow} \lim_{x \rightarrow \infty} \frac{\frac{7x^6}{x^7}}{1} = \lim_{x \rightarrow \infty} \frac{7}{x} = 0$

(100) 4. Calculate the limit $\lim_{x \rightarrow 1} x^{\left(\frac{8}{x-1}\right)}$. $= \lim_{x \rightarrow 1} e^{\ln x^{\left(\frac{8}{x-1}\right)}} = \lim_{x \rightarrow 1} e^{\frac{8}{x-1} \ln(x)}$

Since $\lim_{x \rightarrow 1} \frac{8 \ln x \left(\frac{0}{0}\right)}{x-1} \stackrel{L'H}{=} \lim_{x \rightarrow 1} \frac{\frac{8}{x}}{1} = 8$ $\Rightarrow e^{\lim_{x \rightarrow 1} \frac{8 \ln(x)}{x-1}} = e^8$

and e^x is a continuous function

(∞-∞) 5. Calculate the limit $\lim_{x \rightarrow 0} \left(\frac{8}{x} - 8 \cot(x)\right)$. $\stackrel{(\infty-\infty)}{=} \lim_{x \rightarrow 0} \left(\frac{8 \sin(x) - 8x \cos(x)}{x \sin(x)}\right)$

$\stackrel{(0/0)}{=} \lim_{x \rightarrow 0} \frac{8 \cos(x) - 8 \cos(x) + 8x \sin(x)}{\sin(x) + x \cos(x)}$

$\stackrel{(0/0)}{=} \lim_{x \rightarrow 0} \frac{8 \sin(x) + 8x \cos(x)}{\cos(x) + \cos(x) - x \sin(x)} = \frac{0}{2} = 0$

(∞) 6. Calculate the limit $\lim_{x \rightarrow \infty} (x^6 + 1)^{\frac{1}{\ln(x)}}$. $= \lim_{x \rightarrow \infty} e^{\ln(x^6+1)^{\frac{1}{\ln(x)}}}$

$= \lim_{x \rightarrow \infty} e^{\frac{1}{\ln(x)} \ln(x^6+1)}$

$\Rightarrow e^{\lim_{x \rightarrow \infty} \frac{\ln(x^6+1)}{\ln(x)}} = e^6$

Since $\lim_{x \rightarrow \infty} \frac{\ln(x^6+1)}{\ln(x)}$

$\stackrel{(0/0)}{=} \lim_{x \rightarrow \infty} \frac{\frac{6x^5}{x^6+1}}{\frac{1}{x}}$

$= \lim_{x \rightarrow \infty} \frac{6x^6}{x^6+1} = 6$

↑
(leading coef.)

and e^x is a continuous function