Classwork 5 – Curve Sketching

1. Sketch a graph of a differentiable function f(x) over the closed interval [-2, 7], where f(-2) = f(7) = -3 and f(4) = 3. The roots of f(x) occur at x = 0 and x = 6, and f(x) has the properties indicated in the table below.

Х	-2 <x<0< th=""><th><math>\mathbf{x} = 0</math></th><th>0<x<2< th=""><th>x = 2</th><th>2<x<4< th=""><th>x = 4</th><th>4<x<7< th=""></x<7<></th></x<4<></th></x<2<></th></x<0<>	$\mathbf{x} = 0$	0 <x<2< th=""><th>x = 2</th><th>2<x<4< th=""><th>x = 4</th><th>4<x<7< th=""></x<7<></th></x<4<></th></x<2<>	x = 2	2 <x<4< th=""><th>x = 4</th><th>4<x<7< th=""></x<7<></th></x<4<>	x = 4	4 <x<7< th=""></x<7<>
$f'(\mathbf{x})$	positive	0	positive	1	positive	0	negative
f"(x)	negative	0	positive	0	negative	0	negative
$f(\mathbf{x})$							



- 2. Sketch function h(x) from the following information:
 - a) h(-x) = -h(x)
 - b) $\lim_{\mathbf{x}\to 0^+} \mathbf{h}(\mathbf{x}) = \infty$
 - c) $\lim_{\mathbf{x}\to\infty} \mathbf{h}(\mathbf{x}) = 0$
 - d) for x>0, h(x) = 0 only at x = 1
 - e) for x>0, h'(x) = 0 only at x = 2
 - f) for x>0, h''(x) = 0 only at x = 3

